

## Junior Balkan MO 2007 <br> Shumen, Bulgaria

1 Let $a$ be positive real number such that $a^{3}=6(a+1)$. Prove that the equation $x^{2}+a x+a^{2}-6=$ 0 has no real solution.

2 Let $A B C D$ be a convex quadrilateral with $\angle D A C=\angle B D C=36^{\circ}, \angle C B D=18^{\circ}$ and $\angle B A C=72^{\circ}$. The diagonals and intersect at point $P$. Determine the measure of $\angle A P D$.

3 Given are 50 points in the plane, no three of them belonging to a same line. Each of these points is colored using one of four given colors. Prove that there is a color and at least 130 scalene triangles with vertices of that color.

4 Prove that if $p$ is a prime number, then $7 p+3 p-4$ is not a perfect square.
Comment: This is the official version of the problem, in case you are wondering if I have a typo when writing $7 p+3 p-4$. :D

